

# Meudon initial data for binary black holes

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Meudon data represents quasistationary binary black configurations, obtained by P. Grandclément, E. Gourgoulhon & S. Bonazzola, *Phys. Rev. D* **65**, 044021 (2002).

The exportation of this data, computed by means of LORENE on a multi-domain spectral grid, onto a Cartesian grid (e.g. for CACTUS), is performed by means of the C++ class `Bin_BH`. The class `Bin_BH` comes along with LORENE distribution. This class is very simple, with all data members being public. A typical example of use is the following one

```
* // Define the Cartesian grid by means of the arrays xg, yg, zg:
* for (int i=0; i<nb_points; i++) {
*     xg[i] = ...
*     yg[i] = ...
*     zg[i] = ...
* }
*
* // Read the file containing the spectral data and evaluate
* // all the fields on the Cartesian grid :
*
* Bin_BH binary_system(nb_points, xg, yg, zg, fill, datafile) ;
*
* // Extract what you need :
*
* double* gamma_xx = binary_system.g_xx ; // metric coefficient g_xx
*
* double* shift_x = binary_system.beta_x ; // x comp. of shift vector
*
* ...
*
* // Save everything in an ASCII file :
*
* ofstream file_ini("ini.d") ;
* binary_system.save_form(file_ini) ;
* file_ini.close() ;
*
*
```

---

1  
 class **Bin\_BH**

*Binary black hole configuration on a Cartesian grid.*

### Public Members

1.1	double	<b>omega</b>	<i>Orbital angular velocity [unit: <math>a^{-1}</math>]</i> .....	8
1.2	double	<b>dist</b>	<i>Distance between the coordinate centers of two black holes [unit: <math>a</math>]</i> .....	8
1.3	double	<b>radius2</b>	<i>Coordinate radius of the apparent horizon (throat) of black hole 2 [unit: <math>a</math>].</i> .....	8
1.4	int	<b>np</b>	<i>Total number of grid points</i> ....	8
1.5	double*	<b>xx</b>	<i>1-D array storing the values of coordinate <math>x</math> of the <b>np</b> grid points [unit: <math>a</math>]</i> .....	9
1.6	double*	<b>yy</b>	<i>1-D array storing the values of coordinate <math>y</math> of the <b>np</b> grid points [unit: <math>a</math>]</i> .....	9
1.7	double*	<b>zz</b>	<i>1-D array storing the values of coordinate <math>z</math> of the <b>np</b> grid points [unit: <math>a</math>]</i> .....	9
1.8	double*	<b>nnn</b>	<i>Lapse function <math>N</math> at the <b>np</b> grid points (1-D array)</i> .....	9
1.9	double*	<b>beta_x</b>	<i>Component <math>\beta^x</math> of the shift vector of corotating coordinates [unit: <math>c</math>]</i>	
1.10	double*	<b>beta_y</b>	<sup>10</sup> <i>Component <math>\beta^y</math> of the shift vector of corotating coordinates [unit: <math>c</math>]</i>	
1.11	double*	<b>beta_z</b>	<sup>10</sup> <i>Component <math>\beta^z</math> of the shift vector of corotating coordinates [unit: <math>c</math>]</i>	
1.12	double*	<b>g_xx</b>	<sup>10</sup> <i>Metric coefficient <math>\gamma_{xx}</math> at the grid points (1-D array)</i> .....	10

1.13	double*	<b>g_xy</b>	Metric coefficient $\gamma_{xy}$ at the grid points (1-D array) .....	11
1.14	double*	<b>g_xz</b>	Metric coefficient $\gamma_{xz}$ at the grid points (1-D array) .....	11
1.15	double*	<b>g_yy</b>	Metric coefficient $\gamma_{yy}$ at the grid points (1-D array) .....	11
1.16	double*	<b>g_yz</b>	Metric coefficient $\gamma_{yz}$ at the grid points (1-D array) .....	11
1.17	double*	<b>g_zz</b>	Metric coefficient $\gamma_{zz}$ at the grid points (1-D array) .....	12
1.18	double*	<b>k_xx</b>	Component $K_{xx}$ of the extrinsic curvature at the grid points (1-D array) [unit: c/a] .....	12
1.19	double*	<b>k_xy</b>	Component $K_{xy}$ of the extrinsic curvature at the grid points (1-D array) [unit: c/a] .....	12
1.20	double*	<b>k_xz</b>	Component $K_{xz}$ of the extrinsic curvature at the grid points (1-D array) [unit: c/a] .....	13
1.21	double*	<b>k_yy</b>	Component $K_{yy}$ of the extrinsic curvature at the grid points (1-D array) [unit: c/a] .....	13
1.22	double*	<b>k_yz</b>	Component $K_{yz}$ of the extrinsic curvature at the grid points (1-D array) [unit: c/a] .....	13
1.23	double*	<b>k_zz</b>	Component $K_{zz}$ of the extrinsic curvature at the grid points (1-D array) [unit: c/a] .....	13
1.24	double*	<b>dpsi_x</b>	First derivative $\partial/\partial x$ of the conformal factor $\Psi$ [unit: $a^{-1}$ ] .....	14
1.25	double*	<b>dpsi_y</b>	First derivative $\partial/\partial y$ of the conformal factor $\Psi$ [unit: $a^{-1}$ ] .....	14
1.26	double*	<b>dpsi_z</b>	First derivative $\partial/\partial z$ of the conformal factor $\Psi$ [unit: $a^{-1}$ ] .....	14
1.27	double*	<b>d2psi_xx</b>	Second derivative $\partial^2/\partial x^2$ of the conformal factor $\Psi$ [unit: $a^{-2}$ ] .	14
1.28	double*	<b>d2psi_xy</b>	Second derivative $\partial^2/\partial x\partial y$ of the conformal factor $\Psi$ [unit: $a^{-2}$ ] .	15

1.29	double*	<b>d2psi_xz</b>	<i>Second derivative <math>\partial^2/\partial x\partial z</math> of the conformal factor <math>\Psi</math> [unit: <math>a^{-2}</math>]</i> .	15
1.30	double*	<b>d2psi_yy</b>	<i>Second derivative <math>\partial^2/\partial y^2</math> of the conformal factor <math>\Psi</math> [unit: <math>a^{-2}</math>]</i> .	15
1.31	double*	<b>d2psi_yz</b>	<i>Second derivative <math>\partial^2/\partial y\partial z</math> of the conformal factor <math>\Psi</math> [unit: <math>a^{-2}</math>]</i> .	15
1.32	double*	<b>d2psi_zz</b>	<i>Second derivative <math>\partial^2/\partial z^2</math> of the conformal factor <math>\Psi</math> [unit: <math>a^{-2}</math>]</i> .	16
1.33		<b>Bin_BH</b> (int nbpnts, const double* xi, const double* yi, const double* zi, int fill, const char* filename, bool mdiff=false)	<i>Constructor from Lorene spectral data.</i> .....	16
1.34		<b>Bin_BH</b> (FILE* )	<i>Constructor from a binary file (previously created by save_bin)</i>	17
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1.38	void	<b>save_bin</b> (FILE* ) const	<i>Save in a binary file.</i> .....	17
1.39	void	<b>save_form</b> (ofstream& ) const	<i>Save in a formatted file.</i> .....	18

### Private Members

1.37	void	<b>alloc_memory</b> ()	<i>Allocate the memory for the arrays <math>g_{ij}</math>, <math>k_{ij}</math>, etc</i> .....	18
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Binary black hole configuration on a Cartesian grid.

A binary black hole system is constructed on a Cartesian grid from data stored in a file resulting from a computation by Grandclement,ourgoulhon and Bonazzola, Phys. Rev. D 65, 044021 (2002).

All the quantities are in units derived from the length scale defined by the coordinate radius  $a$  of black hole 1 apparent horizon (throat).

Importation of Lorene data is performed by means of the constructor

`Bin_BH::Bin_BH(int, const double*, const double*, const double*, const char*)`. This constructor takes general arrays for the location of the Cartesian coordinates  $(x, y, z)$ , i.e. it does not assume that the grid is a uniform one. Note also that these arrays are 1-D, as well as all the metric fields, in order to be use with any ordering of the 3-D storage.

This class is very simple, with all data members being public. A typical example of use is the following one

```
* // Define the Cartesian grid by means of the arrays xg, yg, zg:
* for (int i=0; i<nb_points; i++) {
*     xg[i] = ...
*     yg[i] = ...
*     zg[i] = ...
* }
*
* // Read the file containing the spectral data and evaluate
* // all the fields on the Cartesian grid :
*
* Bin_BH binary_system(nb_points, xg, yg, zg, fill, datafile) ;
*
* // Extract what you need :
*
* double* gamma_xx = binary_system.g_xx ; // metric coefficient g_xx
*
* double* shift_x = binary_system.beta_x ; // x comp. of shift vector
*
* ...
*
* // Save everything in an ASCII file :
*
* ofstream file_ini("ini.d") ;
* binary_system.save_form(file_ini) ;
* file_ini.close() ;
*
*
```

**Version:** \$Id: bin\_bh.h,v 1.10 2010/07/14 16:47:30  
e\_gourgoulhon Exp \$

1.1

double **omega**

*Orbital angular velocity [unit:  $a^{-1}$ ]*

Orbital angular velocity [unit:  $a^{-1}$ ]

1.2

double **dist**

*Distance between the coordinate centers of two black holes [unit:  $a$ ]*

Distance between the coordinate centers of two black holes [unit:  $a$ ]

1.3

double **radius2**

*Coordinate radius of the apparent horizon (throat) of black hole 2 [unit:  $a$ ].*

Coordinate radius of the apparent horizon (throat) of black hole 2 [unit:  $a$ ].  
NB: The coordinate radius of black hole 1 is 1 by definition of the length unit.

1.4

int **np**

*Total number of grid points*

Total number of grid points

1.5

**double\* xx***1-D array storing the values of coordinate x of the np grid points [unit: a]*

1-D array storing the values of coordinate x of the np grid points [unit: a]

1.6

**double\* yy***1-D array storing the values of coordinate y of the np grid points [unit: a]*

1-D array storing the values of coordinate y of the np grid points [unit: a]

1.7

**double\* zz***1-D array storing the values of coordinate z of the np grid points [unit: a]*

1-D array storing the values of coordinate z of the np grid points [unit: a]

1.8

**double\* nnn***Lapse function N at the np grid points (1-D array)*

Lapse function N at the np grid points (1-D array)

**1.9**

double\* **beta\_x**

*Component  $\beta^x$  of the shift vector of corotating coordinates [unit: c]*

Component  $\beta^x$  of the shift vector of corotating coordinates [unit: c]

**1.10**

double\* **beta\_y**

*Component  $\beta^y$  of the shift vector of corotating coordinates [unit: c]*

Component  $\beta^y$  of the shift vector of corotating coordinates [unit: c]

**1.11**

double\* **beta\_z**

*Component  $\beta^z$  of the shift vector of corotating coordinates [unit: c]*

Component  $\beta^z$  of the shift vector of corotating coordinates [unit: c]

**1.12**

double\* **g\_xx**

*Metric coefficient  $\gamma_{xx}$  at the grid points (1-D array)*

Metric coefficient  $\gamma_{xx}$  at the grid points (1-D array)

**1.13**

double\* **g\_xy**

*Metric coefficient  $\gamma_{xy}$  at the grid points (1-D array)*

Metric coefficient  $\gamma_{xy}$  at the grid points (1-D array)

**1.14**

double\* **g\_xz**

*Metric coefficient  $\gamma_{xz}$  at the grid points (1-D array)*

Metric coefficient  $\gamma_{xz}$  at the grid points (1-D array)

**1.15**

double\* **g\_yy**

*Metric coefficient  $\gamma_{yy}$  at the grid points (1-D array)*

Metric coefficient  $\gamma_{yy}$  at the grid points (1-D array)

**1.16**

double\* **g\_yz**

*Metric coefficient  $\gamma_{yz}$  at the grid points (1-D array)*

Metric coefficient  $\gamma_{yz}$  at the grid points (1-D array)

**1.17**`double* g_zz`

*Metric coefficient  $\gamma_{zz}$  at the grid points (1-D array)*

Metric coefficient  $\gamma_{zz}$  at the grid points (1-D array)

**1.18**`double* k_xx`

*Component  $K_{xx}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]*

Component  $K_{xx}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

**1.19**`double* k_xy`

*Component  $K_{xy}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]*

Component  $K_{xy}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

**1.20**`double* k_xz`

*Component  $K_{xz}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]*

Component  $K_{xz}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

**1.21**

double* <b>k_yy</b>
---------------------

Component  $K_{yy}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

Component  $K_{yy}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

**1.22**

double* <b>k_yz</b>
---------------------

Component  $K_{yz}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

Component  $K_{yz}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

**1.23**

double* <b>k_zz</b>
---------------------

Component  $K_{zz}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

Component  $K_{zz}$  of the extrinsic curvature at the grid points (1-D array) [unit:  $c/a$ ]

1.24

**double\* dpsi\_x***First derivative  $\partial/\partial x$  of the conformal factor  $\Psi$  [unit:  $a^{-1}$ ]*First derivative  $\partial/\partial x$  of the conformal factor  $\Psi$  [unit:  $a^{-1}$ ]

1.25

**double\* dpsi\_y***First derivative  $\partial/\partial y$  of the conformal factor  $\Psi$  [unit:  $a^{-1}$ ]*First derivative  $\partial/\partial y$  of the conformal factor  $\Psi$  [unit:  $a^{-1}$ ]

1.26

**double\* dpsi\_z***First derivative  $\partial/\partial z$  of the conformal factor  $\Psi$  [unit:  $a^{-1}$ ]*First derivative  $\partial/\partial z$  of the conformal factor  $\Psi$  [unit:  $a^{-1}$ ]

1.27

**double\* d2psi\_xx***Second derivative  $\partial^2/\partial x^2$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]*Second derivative  $\partial^2/\partial x^2$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]

1.28

**double\* d2psi\_xy***Second derivative  $\partial^2/\partial x\partial y$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]*Second derivative  $\partial^2/\partial x\partial y$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]

1.29

**double\* d2psi\_xz***Second derivative  $\partial^2/\partial x\partial z$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]*Second derivative  $\partial^2/\partial x\partial z$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]

1.30

**double\* d2psi\_yy***Second derivative  $\partial^2/\partial y^2$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]*Second derivative  $\partial^2/\partial y^2$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]

1.31

**double\* d2psi\_yz***Second derivative  $\partial^2/\partial y\partial z$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]*Second derivative  $\partial^2/\partial y\partial z$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]

## 1.32

```
double* d2psi_zz
```

*Second derivative  $\partial^2/\partial z^2$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]*

Second derivative  $\partial^2/\partial z^2$  of the conformal factor  $\Psi$  [unit:  $a^{-2}$ ]

## 1.33

```
Bin_BH (int nbpoints, const double* xi, const double* yi,  
        const double* zi, int fill, const char* filename, bool  
        mdiff=false)
```

*Constructor from Lorene spectral data.*

Constructor from Lorene spectral data.

This constructor takes general arrays `xi`, `yi`, `zi` for the location of the Cartesian coordinates  $(x, y, z)$ , i.e. it does not assume that the grid is a uniform one. These arrays are 1-D to deal with any ordering of a 3-D storage.

**Parameters:**

`nbpoints`  
`xi`

`yi`

`zi`

`fill`

`fill = 0` : all the fields are set to zero

`fill = 1` : the fields are extrapolated from their values "outside" the holes, by means of

`filename`

1.34

**Bin\_BH** (FILE\* )*Constructor from a binary file (previously created by save\_bin)*Constructor from a binary file (previously created by `save_bin`)

1.35

**Bin\_BH** (ifstream& )*Constructor from a formatted file (previously created by save\_form)*Constructor from a formatted file (previously created by `save_form`)

1.36

**~Bin\_BH** ()*Destructor*

Destructor

1.38

void **save\_bin** (FILE\* ) const*Save in a binary file.*Save in a binary file. This file can be subsequently read by the evolution code, or by the constructor `Bin_BH::Bin_BH(FILE* )`.

**1.39**

```
void save_form (ofstream& ) const
```

*Save in a formatted file.*

Save in a formatted file. This file can be subsequently read by the evolution code, or by the constructor `Bin_BH::Bin_BH ifstream&` .

**1.37**

```
void alloc_memory ()
```

*Allocate the memory for the arrays g\_ij, k\_ij, etc*

Allocate the memory for the arrays g\_ij, k\_ij, etc

# Class Graph

